

STATISTICS MODULE

Vishwa Hindu Parishad of America
(DC Chapter)

Shantiniketan Camp 2014

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Statistics/Probability in Ancient India



Mahabharata and Gambling



The Dice Game

- Shakuni, Duryodhana's uncle, "facilitates" a dice game against Yudishthira
- Key observation: dice loaded...game is a cheat!
- Yudishthira loses kingdom and wealth
- Gambles wife and kin into servitude
- Yudishthira and the gambler's fallacy
 - Gambler's fallacy and statistics/probability



Outcome of Dice Game



The Story of Nala and Rituparna



Nala & Rituparna

- **Nala:** skilled charioteer
- **Rituparna:** skilled dice-player
- **Synopsis:** Rituparna asks Nala to teach him the skill of an efficient charioteer. In return, Nala asks to be taught in the art of dice.
- **Outcome:** Nala uses the skill he learned from Rituparna to win back his kingdom from his brother Pushkara (whom he had previously lost his kingdom via poor dice-playing).



Gambling in Ancient India vs. Modern-Day Arbitrage

*“A great man knowing mantra and medicine sees a cockfight in progress. He talks to the owner of the two birds separately in a mysterious way. He tells one that ‘if your bird wins, you give me the amount you bet, and if it loses, I will give you $\frac{2}{3}$ of that amount.’ Then he goes to the owner of the other bird where on those same conditions he promised to pay $\frac{3}{4}$ of the amount. In either case, he earned a profit of only 12 pieces of gold. **O mathematician [statistician], blessed with speech, tell me how much money did the owner of each bird bet.”***

Source: *Ganita Saara Samgraha* (Hindi trans. By L.C. Jain)

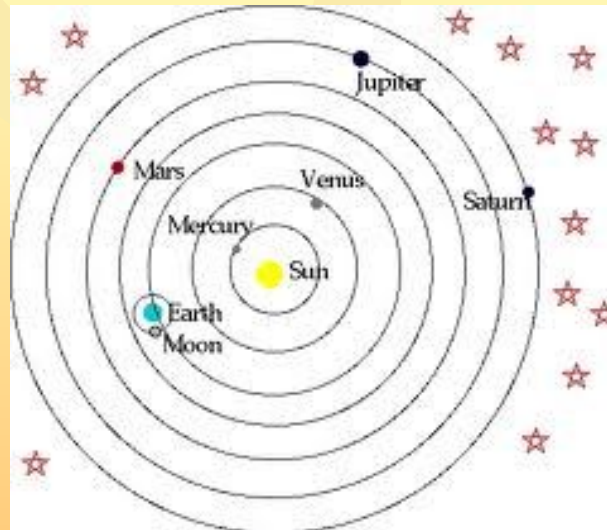


“Statistical Camp”

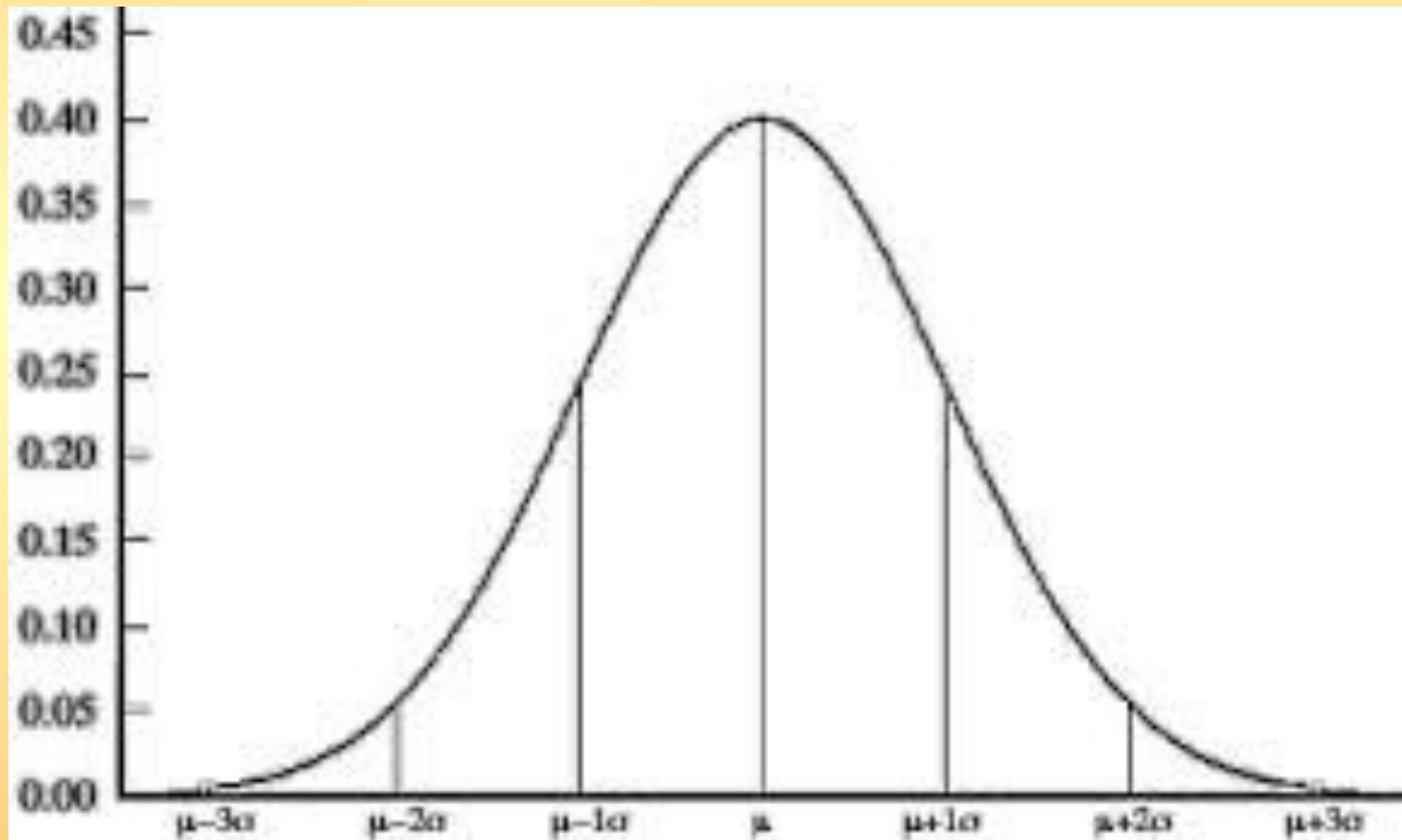


Our Favorite Statistic

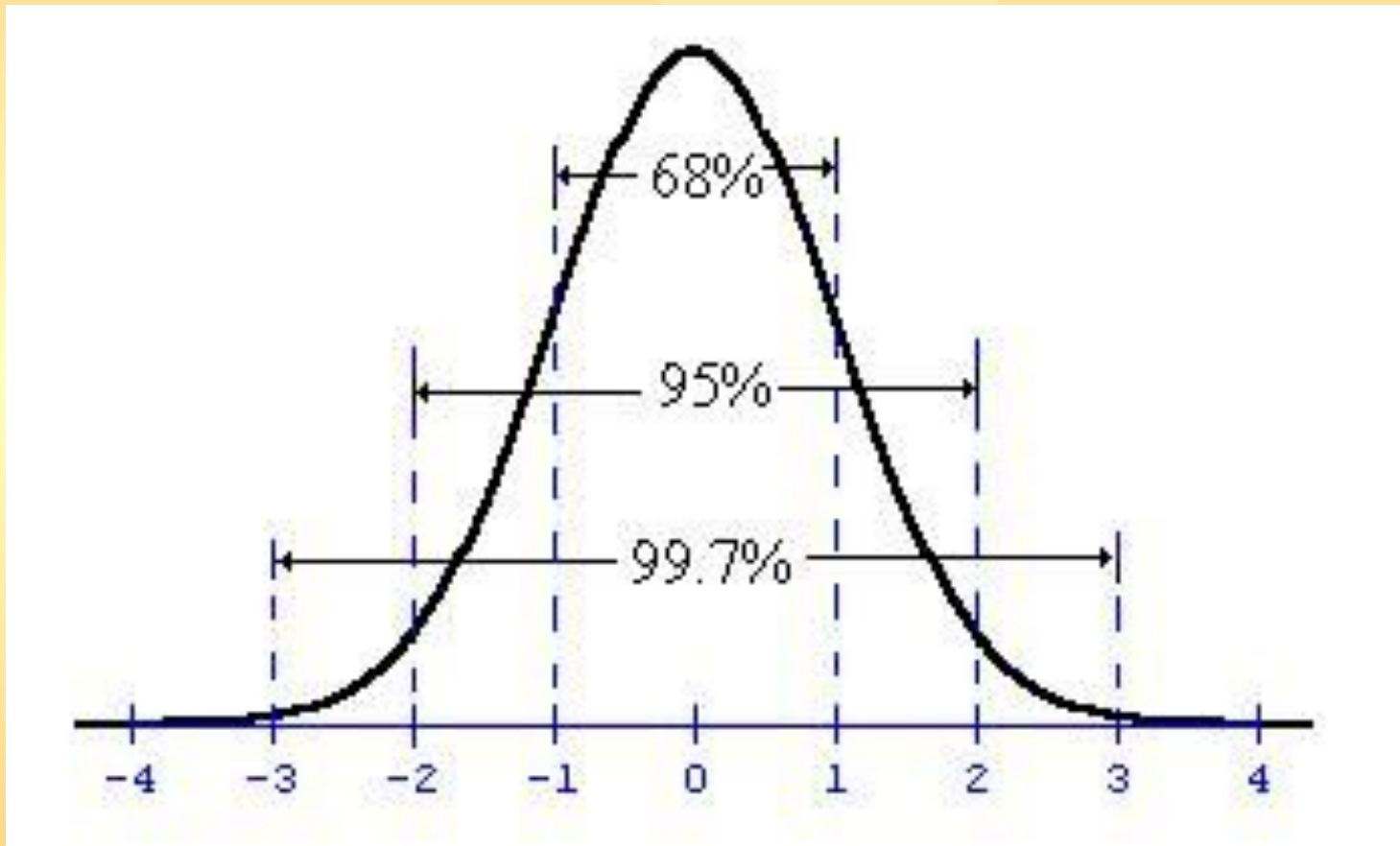
- The average (or the mean)
 - Easy to compute
- Indian planetary models used averages
 - Also concerned with *deviations* from average



Our Favorite Distribution: The Normal (Gaussian) Distribution



Standard Normal Distribution



The Birthday Problem: Part I (Questions)

- Q: What is the chance that you share a birthday with someone?
- Q: How many persons would be needed so that the chance is, say, at least 50%?

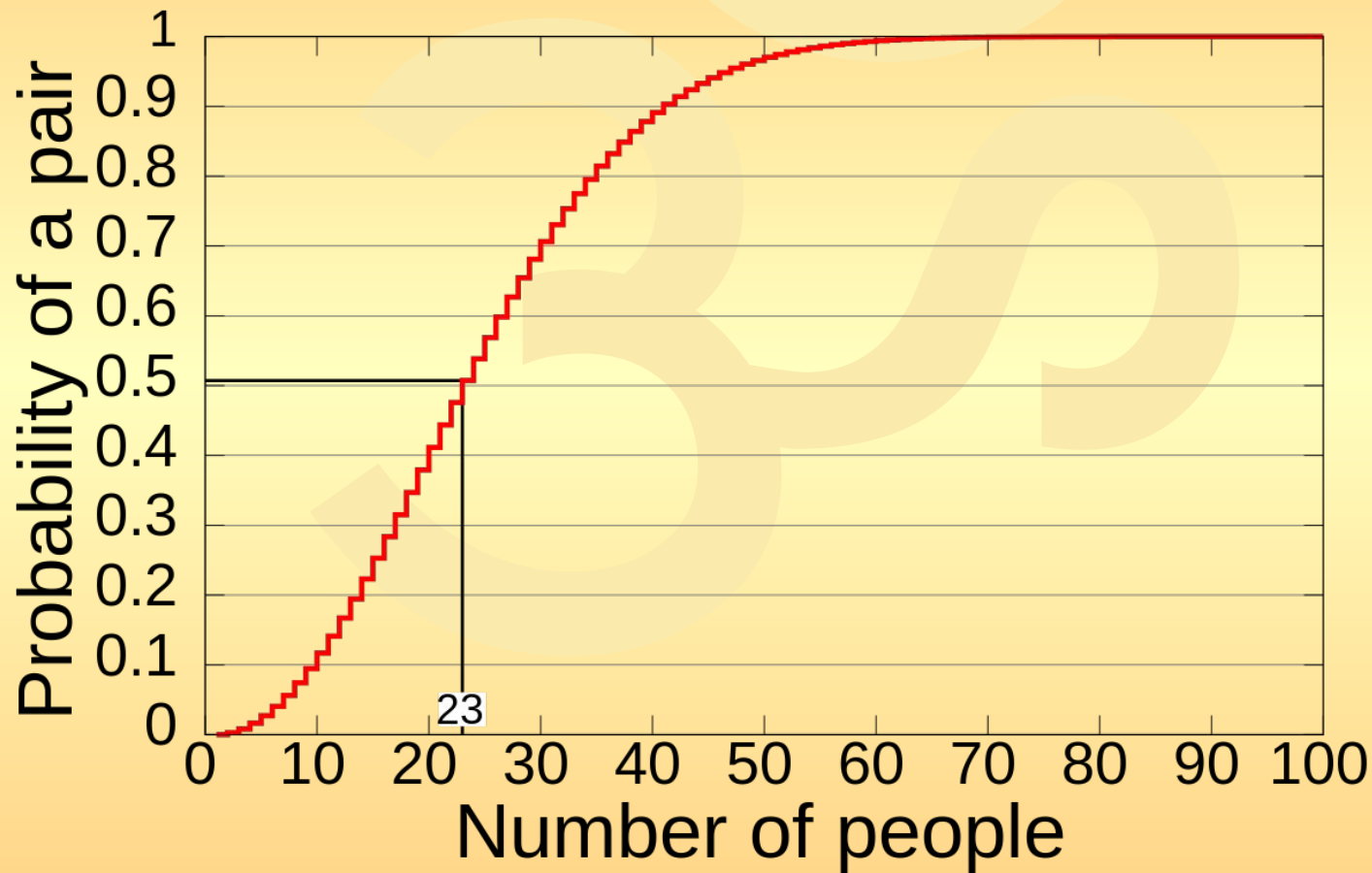


The Birthday Problem: Part II (Solution)

- $\Pr\{\text{at least 2 persons share birthday}\}$
 $= 1 - \Pr\{\text{no persons share birthday}\}$
- Suppose there are n persons. The result is:
 $= 1 - [364/365] \times [363/365] \times \dots \times [(365-n+1)/365]$
 $= p(n)$
- Q: What about those born on Feb. 29th?



The Birthday Problem: Part III (Schematic of $p(n)$)

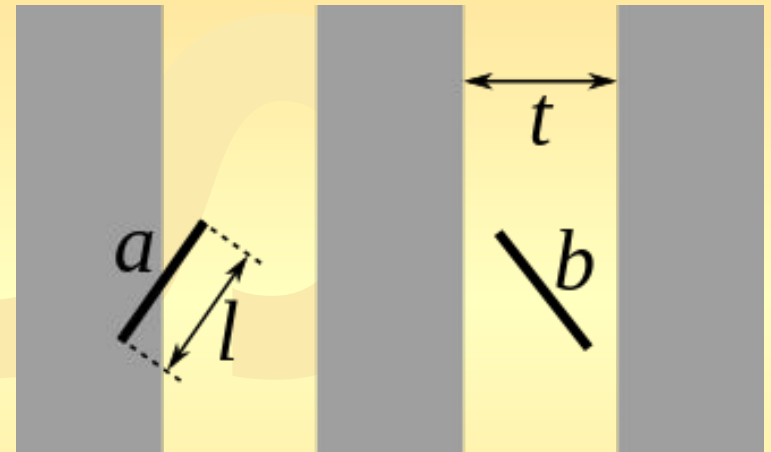


Source:
Wikipedia



Buffon's Needle Problem

- Suppose we have a **floor** made of parallel strips of **wood**, each the same width, and we drop a **needle** onto the floor. What is the **probability** that the needle will lie across a line between two strips?
- How can we use this experiment to estimate the irrational number π ?

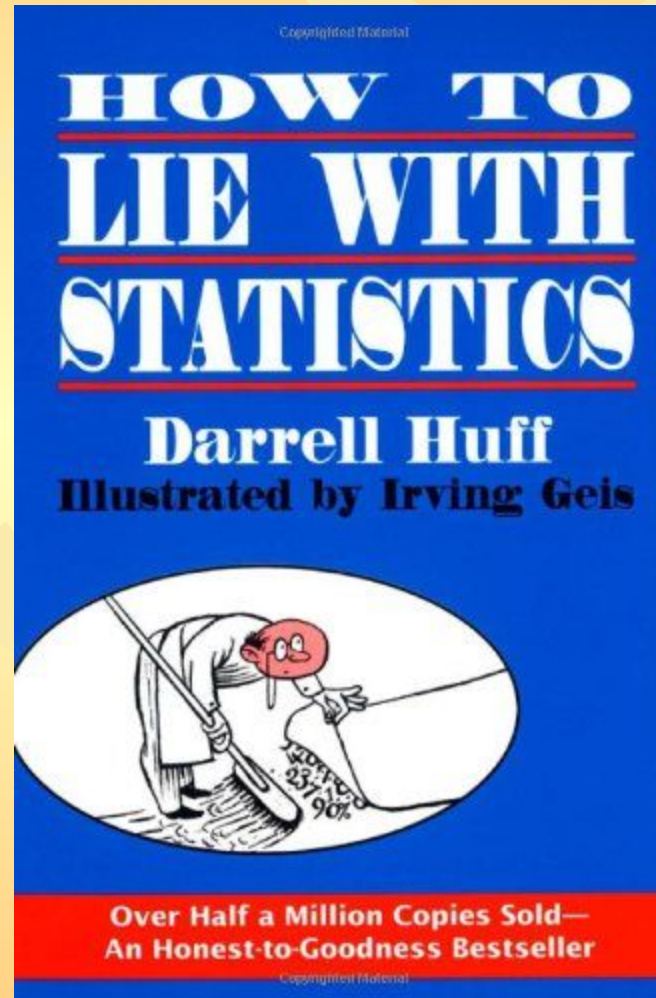


Note: 'needle a' lies across the line while 'needle b' does not.

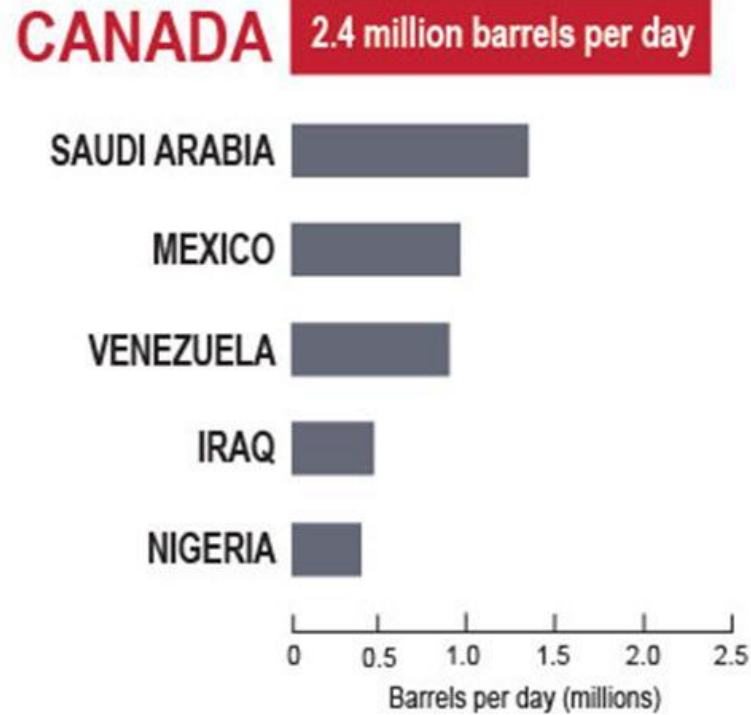
Source:
Wikipedia



How To Lie With Statistics



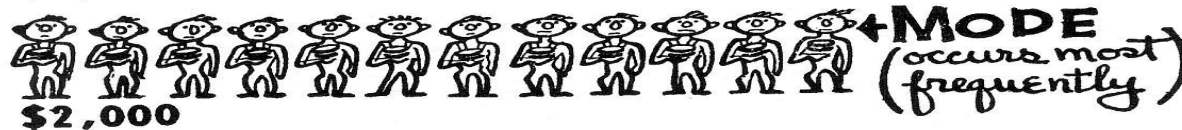
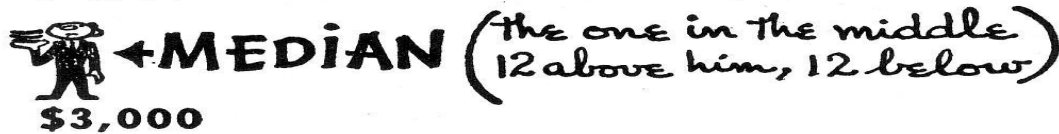
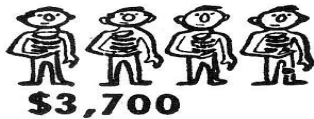
Example: How to Lie -- or Misperlead:



* Source: U.S. Department of Energy, 2013.



A Classic "Lie"

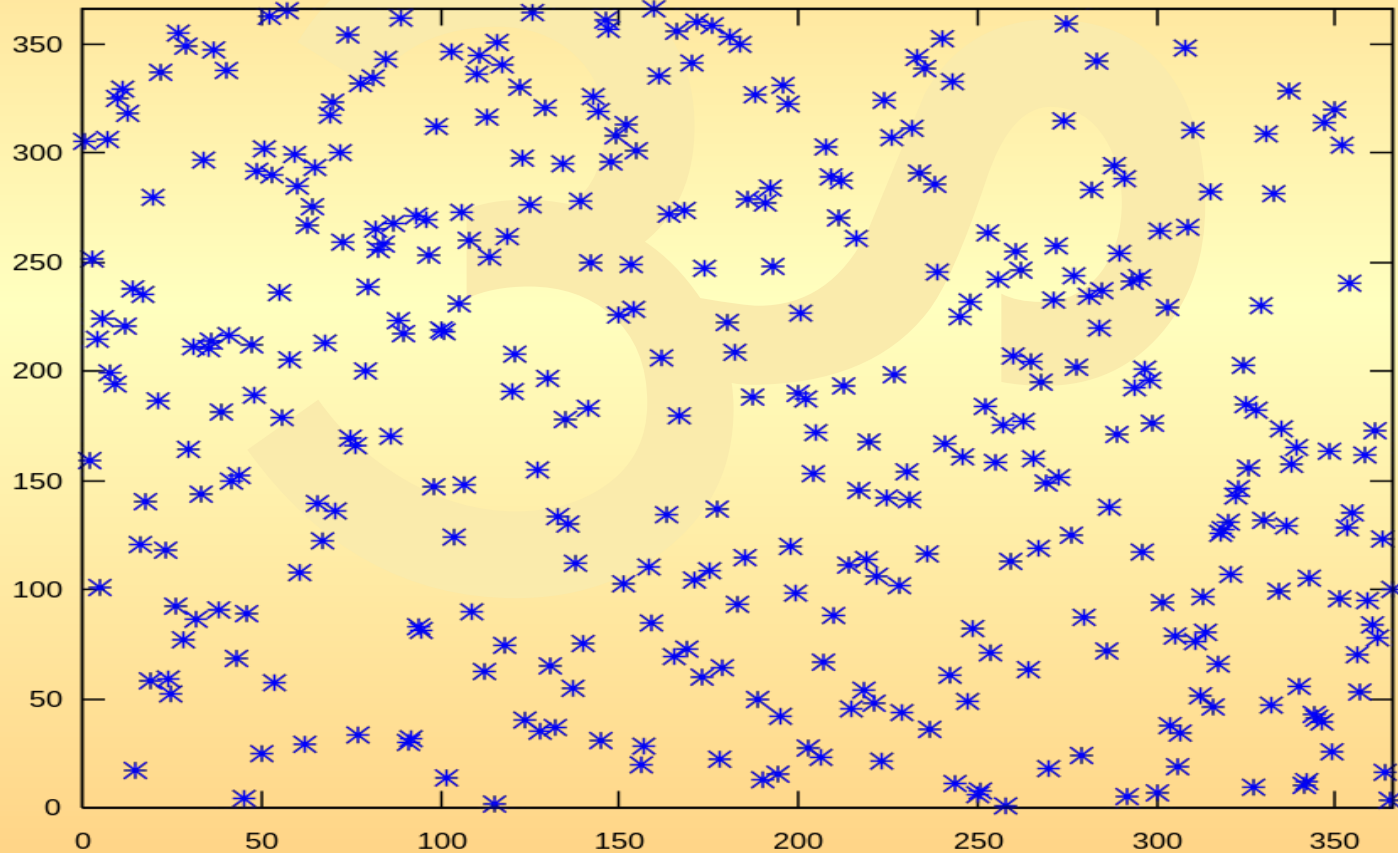


Probability in Action: The Vietnam Draft Lottery of 1969

- Days of the year numbered 1, 2, 3, ..., 366. (Include leap year.)
- Numbers placed in a jar (cf. figure at right).
- Q: Was it fair?
- Q: Are there sources of bias to consider?



Scatter Plot: The Vietnam Draft Lottery of 1969



Famous Indian Statisticians and their Legacies



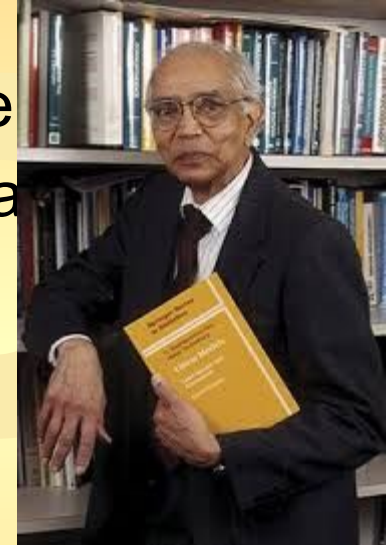
P.C. Mahalanobis

- Birthdate: 29th Jun. 1893
- Birthplace: Calcutta, Bengal
- Education: U. of Calcutta;
Univ. of Cambridge
- **Founder:** Indian Statistical Institute
- Key work area: sample surveys
- Derived the *Mahalanobis Distance*
 - Study of European & Indian marriages
 - Queried which castes married Europeans



Professor C.R. Rao

- Birthdate: 10th Sep. 1920
- Birthplace: Hadagali, Kingdom of Mysore
- Education: Andhra Univ; Univ. of Calcutta
Univ. of Cambridge (PhD, ScD)
- Select accolades:
 - **U.S. Medal of Science**
 - **India Science Award**
- “A living legend” (American Statistical Association)
- Top 10 Indian scientists of all time! (*The Times of India*)
- Derived the *Cramer-Rao Lower Bound*.



The Indian Statistical Institute

- Main campus: Kolkata, West Bengal
- Grew out of Statistical Laboratory from Presidency College, Kolkata set up by P.C. Mahalanobis
- Formed in 1931
- One of India's most prestigious universities -- focus mainly on Statistics (and other fields as well)
- Influenced the establishment of National Institute of Statistical Sciences (NISS) in RTP, North Carolina.



Who Wants to be a Statistician? (Possible Career Paths)



Some “Compelling” Reasons

- Math/Stat rated top job in U.S. in 2014 (and in previous years, too. Source: *Forbes*)
- “Interdisciplinary charm”
 - “Statisticians get to play in everyone’s backyard” (Source: Prof. John Tukey)
 - “Statistics is not a discipline like physics, chemistry or biology where we study a subject to solve problems in the same subject. We study statistics with the main aim of solving problems in other disciplines.” (Source: Prof. C.R. Rao)
- More than just a “number cruncher”



Academia

- College/University professors
 - Tenure-track
 - Teaching track
- Research scientists
 - Laboratories
 - Medical schools
- Consulting center



Federal / Civil Service

- National Statistics Office
 - U.S. Census Bureau
 - Bureau of Labor Statistics
- U.S. Department of Agriculture
 - National Agriculture Statistics Service
 - Recall the *Kaniyaa* and ancient Indian farms
- Military branches
- Economic agencies



Private Sector

- Banking industry
 - Quantitative analysts / researchers
- Hedge funds
 - “Wall Street quants”
 - Goal: seek out arbitrage (recall Nala/Rituparna)
- Multilateral institutions
 - World Bank, IMF, IADB
- Actuarial Science



Statisticians & the “New MBA”

- Computational Finance / Quantitative Finance
- Statistical programming / computing
- Probabilistic arbitrage opportunities
- New breed of “quantitative MBAs”



Parting Quote...Somewhat Ironic... But True!

**“All models are wrong, but some are
useful.”**

(Source: Prof. George E.P. Box)

